

Model Checking LTL over the finite horizon

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AWS

Linear-temporal logic over finite horizon (LTLf)

[Baier and McIlraith; 2006][De Giacomo and Vardi; IJCAI 2013]

- Specification language
 - Temporal logic over discrete time
- Syntax
 - Boolean variables and operators
 - Temporal operators: Always, Eventually, Next, Until ...

Example: Always (Request \rightarrow (Grant \vee Next Grant))

- “Every request is granted within the two steps”

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Request	T	F	T	F	T	T
Grant	T	F	F	T	F	T



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Prior works on LTLf

Planning

Reactive
Synthesis

Reinforcement
Learning

Satisfiability

Model
Checking
???

LTL vs. LTLf

LTLf is at most as hard as LTL, if not easier

	LTL	LTLf
Deterministic automata	(DPA) 2 Exponential	(DFA) 2 Exponential
Satisfiability	PSPACE-complete	PSPACE-complete
Synthesis	2EXPTIME-complete	2EXPTIME-complete

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Model Checking	PSPACE-complete	EXPSPACE-complete

LTL model checking

[Vardi and Woolper; LICS 1986]

Model M satisfies LTL specification ψ if

Every execution of model satisfies ψ

$$M \subseteq \psi \quad \text{iff} \quad M \cap \neg\psi = \emptyset$$


Counterexamples

LTL model checking is PSPACE-complete

The issue with LTLf model checking

Model M satisfies LTLf specification ψ if

Every execution of model satisfies ψ



Executions are of
Infinite-length



Defined over finite-
length executions



Non-terminating models are without terminating states

- Model checking of LTL is on non-terminating models
- Generated by most LTLf reactive synthesis algorithms/tool

LTLf model checking

Model M satisfies LTLf specification ψ if

Every execution of model **has a prefix** that satisfies ψ

$$M \subseteq \underbrace{\exists \text{ prefix, prefix satisfies } \psi}_{\text{Words of infinite-length}}$$

$$(M \cap \underbrace{\forall \text{ prefix, prefix satisfies } \neg \psi}_{\text{Counterexamples}}) = \emptyset$$

Complexity

Given LTLf formula ψ , generate counterexample automata

- Accepts infinite word if all prefixes satisfy $\neg\psi$
- Deterministic form is double exponential in ψ (upper bound)
- Non-deterministic form is also double exponential in ψ (lower bound)
 - Universal quantification on prefixes
 - LTLf can identify **Last** of a finite execution
 - Intuition: (For every prefix, **Last** a) \equiv (**Globally** a) in LTL

Theorem.

For non-terminating models, LTLf model checking is EXPSPACE-hard

In a nutshell

Model Checking LTL over the Finite Horizon

- Among the first to study model checking of LTLf specifications
- For non-terminating models, LTLf model checking is EXPSPACE-hard
- For terminating models, LTLf model checking is PSPACE-hard
- Efficient and scalable algorithms for LTLf model checking
- Busted the myth that LTLf is easier than LTL: Examine implications